

THIRD SEMESTER **B.C.A.** DEGREE EXAMINATION, NOVEMBER 2012

(CCSS)

## CA 3C 06—OPERATIONS RESEARCH

Time : Three Hours

Maximum : 30 **Weightage**I. Answer all *twelve* questions

- 1 Any solution of **LPP** which satisfies the non-negativity constraint is called \_\_\_\_\_
- 2 The maximization problem in the primal become the \_\_\_\_\_ problem in dual.
- 3 If a constant value is added to every cost element  $c_{ij}$  in the transportation problem, the optimal value of the variables  $x_{ij}$  will change. Is it true ?
- 4 If the cost matrix of a given assignment problem is not a square matrix, then the problem is \_\_\_\_\_
- 5 In a traveling salesman problem, the salesman can visit a city twice, until he has visited all the cities once—Is it true or false.
- 6 The time between starting the first job and completing the last job which also include the ideal time is \_\_\_\_\_
- 7 What is the name of the activity whose total float is zero.
- 8 The time period over which the inventory level will be controlled is known as \_\_\_\_\_
- 9 The optimum order quantity decreases with increase in \_\_\_\_\_
- 10 If all the items are replaced irrespective of whether they have failed or not is known as \_\_\_\_\_ policy. \_\_\_\_\_
- 11 The ordering cost is independent of \_\_\_\_\_
- 12 The time period between placement of two successive orders is referred to as \_\_\_\_\_

(12 x = 3 **weightage**)II. Answer *all* questions :

- 13 Convert the following
- LPP**
- into standard form :

$$\text{Minimize } Z = 3x_1 + 2x_2$$

$$\text{subjected to } 4x_1 + 3x_2 \leq 12$$

$$4x_1 + x_2 \geq 2$$

$$x_1, x_2 \geq 0.$$

- 14 What is
- pseudo-optimal**
- solution.

Turn over

15 Write the dual of the following LPP

$$\text{Maximize } Z = 3x_1 - x_2 + x_3$$

$$\text{subjected to } 4x_1 - x_2 \leq 8$$

$$8x_1 + 4x_2 + x_3 \geq 2$$

$$x_2 \geq 0.$$

16 Define basic solution and optimal basic feasible solution.

17 Obtain an initial basic solution for the following transportation problem using least cost method.

18 Determine an initial basic feasible solution for the following transportation problem using least cost method

	I	50	30	220	1
From	II	90	45	170	3
	III	250	200	50	4
		4			
					Availability

19 Solve the following minimal assignment problem :

			Men			
			1	2	3	4
	I	12	30	21	15	
Job	II	18	33	9	31	
	III	44	25	24	21	
	IV	23	30	28	14	

20 The annual demand for a product is 1,00,000 units. The rate of production is 2,00,000 units per year. The set-up cost per production run is Rs. 5,000 and the variable product cost of each item is Rs. 10. The annual holding cost per unit is 20% of its value. Find the optimum production for size and the length of the production run.

21 Draw a network and determine the critical path :

Job	:	1-2	1-3	2-4	3-4	3-5	4-5	4-6	5-6
Duration	:	6	5	10	3	4	6	2	9

Draw a network and find the critical path.

(9 x 1 = 9 weightage)

III. Answer any *five* questions :

22 A resourceful home decorator manufactures 2 types of lamps say A and B. Both lamps go through two technicians first a cutter and second finisher. Lamp A requires two hours of cutter's time and one hour of the finisher's time. Lamp B requires one hour of cutter's time and two hours of finishers time. The cutter has 104 hours and finisher has 76 hours of available time each month. Profit on 1 lamp A is Rs. 6 and on one lamp B is R. 11. Formula a mathematical model, to the problem.

23 Solve by simplex method ;

$$\text{Maximize } Z = 7x_1 + 5x_2$$

$$\text{subjected to } x_1 + 2x_2 \leq 6$$

$$4x_1 + 3x_2 \leq 12$$

$$x_1, x_2 \geq 0.$$

24 Solve the Transportation problem by **Vogal** Approximation Method

	1	2	3	4	
	1	2	3	4	6
2	4	3	2	0	8
3	0	2	2	1	10
	4	6	8	6	

25 The probability  $P_n$  of failure just before age n is shown below. An individual replacement cost Rs. 12.5 and group replacement costs Rs. 3 per item. Find the optimal replacement policy

n	1	2	3	4	5
$P_n$	0.1	0.2	0.25	0.3	0.15

26 The following table shows the jobs of a network along with their time estimates. The time estimates are in days.

Job	1-2	1-6	2-3	2-4	3-5	4-5	5-8	6-7	7-8
a	3	2	6	2	5	3	1	3	4
m	6	5	12	5	11	6	4	9	19
b	15	14	30	8	17	15	7	27	28

Turn over

27 A conductor has to supply 20,000 unit per day. He can produce 30,000 units / day. The cost of holding a unit is stock is Rs. 3 per year and the set-up cost per run is Rs. 50. How frequently and of what size should the production run be made.

28 Draw a network and determine the critical path :

Job	1-2	1-3	2-4	3-4	3-5	4-5	4-6	5-6
Duration	6	5	10	2	4	6	2	9

(5 x 2 = 10 weightage)

N. Answer any two questions :

29 Use penalty method (Big M method) solve the following LPP :

$$\text{Maximize } Z = 2x_1 + x_2 + 3x_3$$

$$\text{subjected to } x_1 + x_2 + 2x_3 = 5$$

$$2x_1 + 3x_2 + 4x_3 = 12$$

$$x_1, x_2, x_3 \geq 0$$

30 A machine operator has to perform three operations turning, threading and knurling on a number of different jobs. The time required to perform these operations (in minutes) of each job is known. Determine the order in which the jobs should be processed in order to minimize the total time required to turn out all the jobs.

Job	1	2	3	4	5	6
Turning	3	12	5	2	9	11
Threading	8	6	4	6	3	1
Knurling	13	14	9	12	8	13

31 Solve the transportation problem :

		Destination				Supply
		A	B	C	D	
Source	1	11	20	7	8	50
	2	21	16	20	12	40
	3	8	12	8	9	70
Demand		30	25	35	40	

(2 x 4 = 8 weightage)