

SECOND SEMESTER (CUCBCSS—UG) DEGREE EXAMINATION, MAY 2019

B.C.A.

BCA 2C 03—COMPUTER ORIENTED STATISTICAL METHODS

(2014 Admissions)

Time : Three Hours

Maximum : 80 Marks

Part A

Answer **all** questions.

Each question carries 1 mark.

1. Sum of deviations observations from their arithmetic mean is _____
2. _____ is the graphical method studying dispersion.
3. Set of all possible outcomes of a random experiment is known as _____
4. Three unbiased coins are tossed _____ is the probability of getting at least one head.
5. Two random variables are said to be independent if $f(x, y) =$ _____
6. A distribution for which mean is greater than variance is _____
7. Standard deviation of sampling distribution of a statistic is called _____
8. The square of Standard. Normal distribution is _____
9. The joint distribution of sample observations is called _____
10. If t_n is consistent for 0, t_{n^2} is consistent. for _____

(10 x 1 = 10 marks)

Part B (Short Answer Type Questions)

Answer **all** questions.

Each question carries 2 marks.

11. For any *two* positive numbers, prove that $AH = G^2$, where A is the arithmetic mean, G is the geometric mean, and H is the harmonic mean.
12. Give classical definition of probability.
13. Define random variable and give two examples.

Turn over

14. Define F-statistic.

15. What is meant by a statistical hypothesis? Explain simple and composite hypothesis.

(5 x 2 = 10 marks)

Part C (Short Essay Type Questions)

Answer any five questions.

Each question carries 4 marks,

16. Explain the method of constructing a Lorenz curve.

17. Prove that standard deviation is independent of change of origin, but not of scale.

18. Let $B \subset A$, prove that (i) $P(A \cap B^c) = P(A) - P(B)$; and (ii) $P(B) \leq P(A)$.

19. The p.d.f. of a random variable X is given by $f(x) = kx(1-x)$; $0 < x < 1$:

(i) Find the value of k .

(ii) Obtain the distribution function of X .

20. Define the moment generating function of a random variable. Explain how you will obtain moments from a moment generating function.

21. Obtain the sampling distribution of mean of the samples from a Normal population.

22. Obtain the interval estimate of variance of a Normal population.

23. Obtain the maximum likelihood estimator of parameter of a Poisson population.

(5 x 4 = 20 marks)

Part D (Essay Questions)

Answer any five questions.

Each question carries 8 marks.

24. Obtain the coefficient of variation for following data :

Length of life (in hours) :	500-700	700-900	900-1100	1100-1300	1300-1500
No. of bulbs	5	11	26	10	8

25. Fit a straight line to the following data :

Year	1992	1994	1996	1998	2000	2002	2004
Production	77	81	88	94	94	96	98

26. Find the co-efficient of correlation between X and Y from the following data :

X	15.5	16.5	17.5	18.5	19.5	20.5
	75	60	50	50	45	40

27. The two lines of regression are given by $8x - 10y - 66 = 0$ and $40x - 18y = 214$:

- Identify the regression lines.
- Find the mean values of X and Y.
- Find the correlation co-efficient between X and Y.
- Find the standard deviation of Y, if the standard deviation of X is 3.

28. From a group of 3 Indians, 4 Pakistanis and 5 Americans, a sub-committee of four peoples is selected by lots. Find the probabilities that the sub-committee will consist of :

- 2 Indians and 2 Pakistanis.
- 1 Indian, 1 Pakistani and 2 Americans.
- At least one Indian.

29. A random variable X has the p.m.f. given by :

X	-3	-1	0	1	2	3
f(x)	k^2	$2k^2 + k$	$2k^2 + 3k$	$4k^2 + 5k$	$3k^2 + 3k$	$2k^2 + k$

- Find the value of k.
- Obtain the distribution function of X
- Find $P(X > 1)$ and $P(X \leq 2)$.

30. From a Normal population $N(\mu, \sigma^2)$, obtain :

- The MLE of p when σ^2 is known.
- The MLE of σ^2 when μ is known.

31. Let x_1, x_2, \dots, x_9 is a random sample of size nine taken from a Normal population $N(25)$. To test

$H_0 : \mu = 5$ against $H_1 : \mu = 6$, the critical region suggested is $\bar{x} > 7$ where \bar{x} is the sample mean.

Find the significant level and power of the test.

(5 x 8 = 40 marks)