

FIRST SEMESTER **B.C.A.** DEGREE EXAMINATION, JANUARY 2013

(CCSS)

BCA

CA 10 02—DISCRETE MATHEMATICS

Time : Three Hours _____

Maximum : 30 Weightage

Part A (Objective Type Questions)

*Answer all twelve questions.*1. The value of $c(n, n)$ is :

(a) 1.

(b) n .

(c) 0.

(d) $n!$.2. What is the order of the recurrence relation $a_r - 6a_{r-1} = 0, r \geq 1$.

(a) 0.

(b) 1.

(c) 2. _____

(d) 6.

3. Example of a group of four elements.

(a) S_4 .

(b) Klein group.

(c) Set of integers less than under addition.

(d) Z_4 under multiplication.4. The value of ${}^nP_{n-1}$ is :(a) n .(b) $n!$.

(c) 1.

(d) $n-1$.5. If $p = F$ and $q = F$ then $p \wedge q$ is _____6. The negation of $\exists x, p(x)$ is _____7. The value of 01 is _____8. Formula for $p(n, r)$ is _____9. If $p = T$ then $p \vee \neg p = F$. True or False.

10. Can every group of prime order a generator ?

Turn

11. Every integral domain is a field. True or False.

12. $c(n, r) = c(n, n - r)$. True or False.

(12 x 1/3 = 4 weightage)

Part B (Short Answer Questions)

Answer all questions.

13. Form the conjunction of :

P : It is raining today.

Q : There are 20 tables in this room.

14. Evaluate $p(n, r)$ for $n = 6$ and $r = 2$.

15. Find the number of ways to paint 12 offices so that 3 of them will be green, 2 of them pink, 2 of them yellow and the **remainings** are white.

16. If $c(n, 9) = c(n, 8)$. Then find c

17. Define commutative ring with example.

18. Write the truth table for conjunction and disjunction.

19. Symbolize the expression

"all the world loves a lover".

20. Suppose a housekeeper wants to schedule spaghetti dinner three times each week. Find the number of ways of scheduling it.

21. If G is group with binary operation $*$ and if a and b are any elements of G . Then show that the linear equation $a * x = b$ and $y * a = b$ have unique solutions in G .

(9 x 1 = 9 weightage)

Part C (Short Essay Questions)

Answer any five questions.

If $a = a_0 + a_1r + a_2r^2 + \dots + a_n r^n$, show that $a = o(r^n)$.

If $\frac{1}{8!} + \frac{1}{9!} = \frac{x}{10!}$ find x .

Find the value of n such that $p(n, 5) = 42 p(n, 3)$.

Show that every field F is an integral domain.

State and prove division algorithm for Z .

27. Find the truth table for $(p \vee Q) \vee p$.

28. Let $a = r + O(1/r)$ and $b = \sqrt{r} + O(1/r)$. Show that $ab = r^{3/2} + O(r^{1/2})$.

(5 x 2 = 10 weightage)

Part D (Essay Questions)

Answer any two questions.

29. Solve the equations :

$$a_n = 3a_{n-1} + 2b_{n-1} \text{ and}$$

$$b_n = a_n + b_{n-1} \text{ with the}$$

boundary conditions $a_0 = 1$ and $b_0 = 0$.

30. If \mathbf{R} is a ring with additive identity 0, then for any $a, b \in \mathbf{R}$, we have

(a) $0 \cdot a = a \cdot 0 = 0$.

(b) $a(-b) = (-a)b = -(ab)$.

(c) $(-a)(-b) = ab$.

31. Write the truth table for $\sim(p \wedge Q)$ and $(\sim p \vee Q)$ and verify them.

(2 x 4 = 8 weightage)